number of gaps is

$$P = \int_N^{N'} dx / \log x,$$

while the number for g = 2 or for g = 4 is the well-known

$$E_2 = E_4 = 1.3203236317 \int_N^{N'} dx / \log^2 x.$$

For larger g, Brent uses his formulae developed in [1].

The first 21 tables are for the intervals

$$(10^{i}, 10^{i} + 10^{6}), \qquad j = 6(1)15;$$

$$(10^{i}, 10^{i} + 10^{7}), \qquad j = 7(1)14;$$

$$(10^{6}, 10^{i}), \qquad j = 7, 8, 9.$$

For each interval there is listed the first and last prime; the observed population for each g: O_{p} ; the expected number E_{p} for g = 2(2)80 according to the aforementioned formulas; the expected number for $g > 80 = P - \sum_{2}^{80} E_{p}$; the normalized differences $(O_{p} - E_{p})/(E_{p})^{1/2}$; and a χ^{2} computed for these 41 degrees of freedom. The χ^{2} vary from 20 to 73 and seem to suggest that, if anything, the distribution agrees "too well" with the expected distribution.

For the remaining four intervals

$$(10^{i}, 10^{i} + 2 \cdot 10^{i}), \quad j = 15, 16,$$

 $(10^{i}, 10^{i} + 10^{8}), \quad j = 14, 16,$

only the empirical data are given, not the expected values or χ^2 .

There is included a 13-page Fortran and 360 Assembly Language program. One sees that the estimating integrals were computed with a 16-point Gauss integration. There also is a 3-page text.

The empirical counts in the interval $(10^{14}, 10^{14} + 10^8)$ were tabulated earlier by Weintraub [2]. The data agree.

D. S.

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- 8 [9].—EDGAR KARST, The Third 2500 Reciprocals and their Partial Sums of all Twin Primes (p, p + 2) between (239429, 239431) and (393077, 393079), University Computer Center, The University of Arizona, Tucson, Arizona, February 1973. Ms. of 207 computer sheets deposited in the UMT file.
- 9 [9].—DANIEL SHANKS & CAROL NEILD, Brun's Constant, Computation and Mathematics Department, Naval Ship Research and Development Center, Bethesda, Maryland, April 1973. Ms. of 67 computer sheets deposited in the UMT file. For a detailed review of these unpublished tables, see pp. 295–296 of this issue.

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